

(Following Paper ID and Roll No. to be filled in your Answer Books)

Paper ID :120661

Roll No.

B.TECH.

Theory Examination (Semester-VI) 2015-16

DIGITAL CONTROL SYSTEM

Time : 3 Hours

Max. Marks : 100

Section-A

Q.1 Attempt all parts. All parts carry equal marks. Write answer of each part in short. (2×10=20)

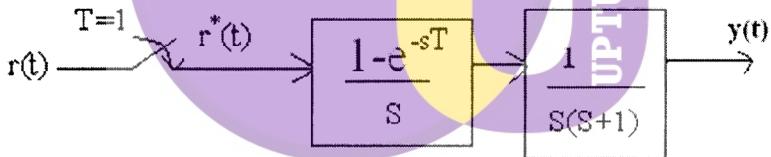
- (a) What are the advantages of digital control over analog control system?
- (b) Discuss the importance of ROC a digital system.
- (c) What are the limitations of high-gain in feedback control system?
- (d) State Cayley-Hamilton theorem.
- (e) What is difference between open loop and close loop system?
- (f) Define State Transition matrix.

- (g) Define bilinear transformation.
- (h) Define Routh stability criterion for right-half s-Plane.
- (i) Define poles and zeros? Explain its significance.
- (j) Draw sample and hold circuit.

Section-B

Q2. Attempt any 5 questions from this section. (10×5=50)

- (a) Describe the configuration of the basic Digital control scheme & explain the importance of each building blocks.
- (b) Find the response of the system shown in figure to a unit impulse input.



- (c) Write the rules for construction of root locus plot of $1+F(z)$ in digital compensator design.
- (d) Convert the following transfer function to state variable model using (i) first companion form, (ii) second companion form and (iii) Jordan Canonical form.

$$G(S) = \frac{s + 3}{S^3 + 9S^2 + 24S + 20}$$

- e) Using jury stability criterion, find all the poles of the following transfer function lie inside the circle the unit circle on the z-plane.

$$G(Z) = \frac{3z^4 + 2z^3 - z^2 + 4z + 5}{z^4 + 0.5z^3 + -0.2z^2 + z + 0.4}$$

- f) State the liapunov's main theorem. Examine the stability of the system described by

$$\dot{X}_1 = X_2 - X_1(X_1^2 + X_2^2)$$

$$\dot{X}_2 = -X_1 - X_2(X_1^2 + X_2^2)$$

- g) State and explain the Max. Min. principle. Describe its performance index.

- h) Find the optimal control $u^*(t)$ for the $\dot{x} = u$; $x(0)=1$

which minimizes $J = \frac{1}{2}x^2(4) + \frac{1}{2}\int_0^4 u^2 dt$.

Section-C

Note: Attempt any 2 questions from this section.

(15×2=30)

- Q3. Consider the digital control system shown in figure 1, the transfer

function of the plant is $G(s) = \frac{1}{S(s+1)}$

Design a lead compensator $D(z)$ in the w -plane such that the phase margin is 50° , the gain margin is at least 10 dB, and the velocity error constant K_v is 2. Assume that the sampling period is 0.2 sec.

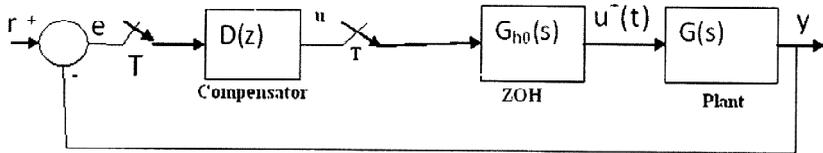


Figure 1

- Q4. (a) Define stability of digital control system and discuss how is jury-stability criterion applied for stability investigation for such systems.
- (b) Check stability of the digital control system shown by its block diagram in figure 2.

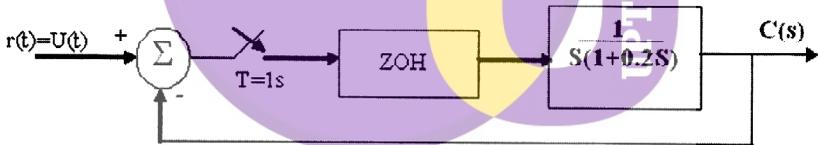


Figure 2

- Q5. (a) State the principle of optimality. Also derive the dynamic programming equation.
- (b) State and explain the concept of dynamic programming.